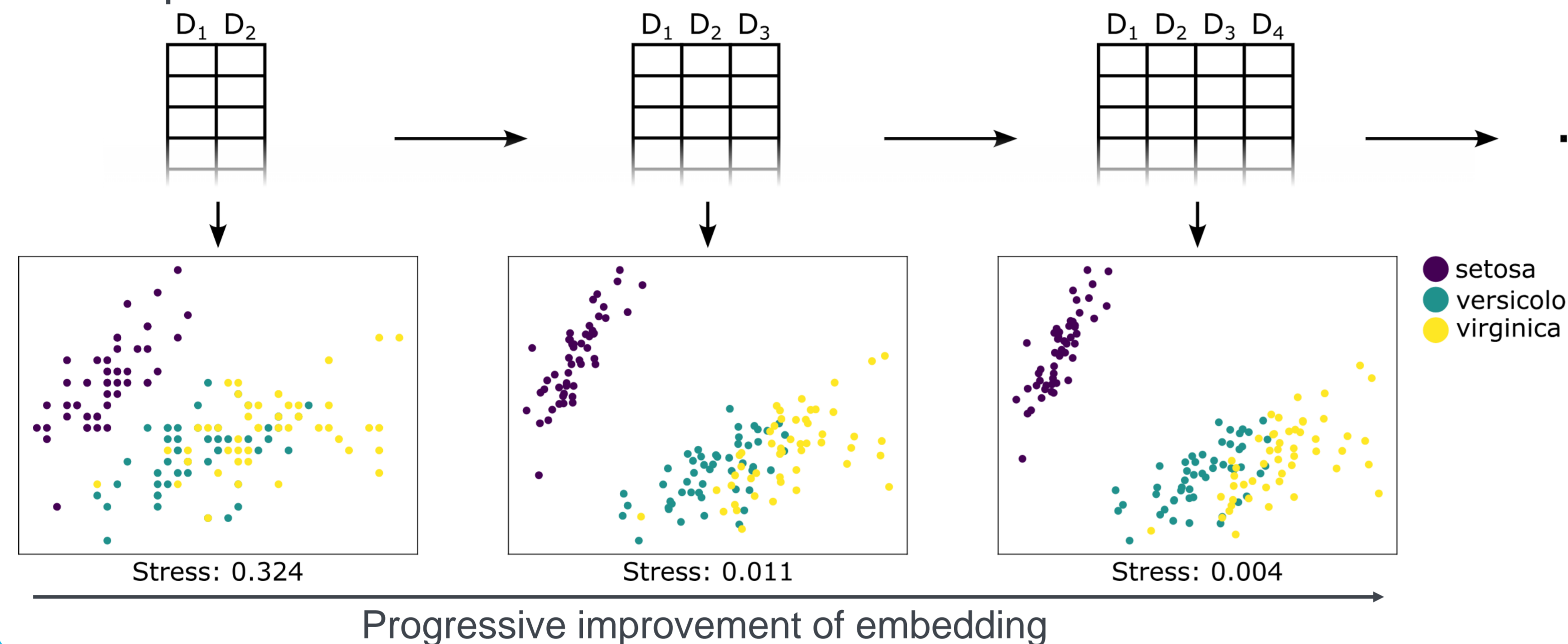


Goal

Progressive updates to an MDS embedding for changes in the data's dimensionality

Algorithm

- Builds on Glimmer [1]
- Initial condition: two dimensions or running Glimmer on the first set of dimensions
- Use results with fewer dimensions as a starting point
- Avoid hierarchical processing and use Chalmers' algorithm directly
- Adapt termination criterion because fewer iterations often suffice



Algorithm 1 Progressive Glimmer

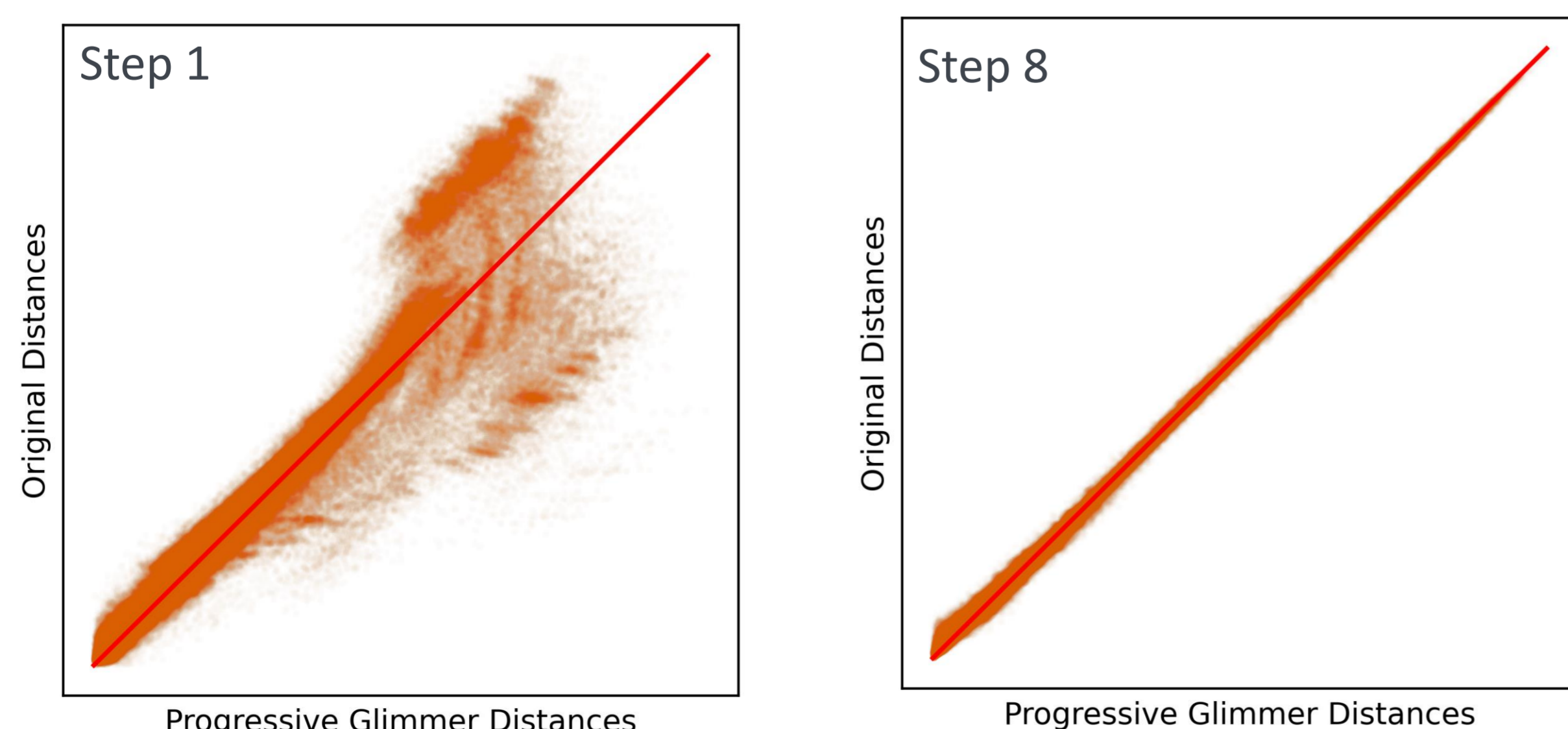
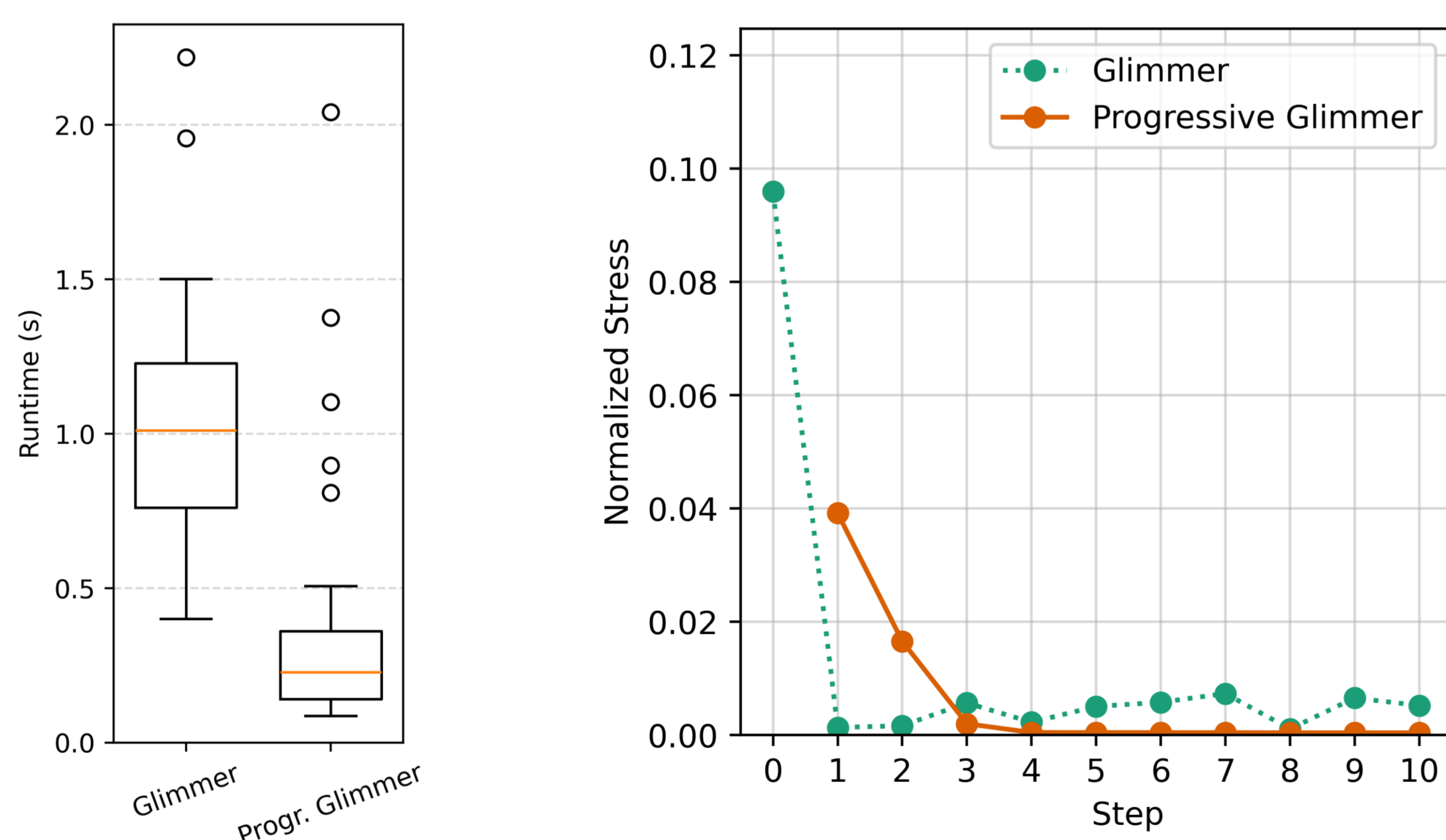
```

1:  $X \leftarrow \text{data}[\text{dim}_1 \dots \text{dim}_l]$ 
2:  $Y \leftarrow \text{data}[\text{dim}_1, \text{dim}_2]$ 
3:  $\mathcal{N} \leftarrow$  random set of  $k$  neighbors for each  $x \in X$ 
4: CHALMERS-MDS( $X, Y, \mathcal{N}$ )
5: extend  $X$  with more dimensions, repeat previous step
6: procedure CHALMERS-MDS( $X, Y, \mathcal{N}$ )
7:    $\delta \leftarrow$  initial forces set to 0
8:    $s = []$ 
9:   while has not converged do
10:    LAYOUT( $X, Y, \mathcal{N}, \delta$ )
11:    append current stress to  $s$ 
12:     $\mathcal{N}' \leftarrow$  random set of  $k/2$  neighbors for each  $x \in X$ 
13:     $\mathcal{N} \leftarrow$  keep close neighbors, replace others by  $\mathcal{N}'$ 
14:   end while
15: end procedure
16: procedure LAYOUT( $X, Y, \mathcal{N}, \delta$ )
17:   stress  $\leftarrow$  0
18:   for  $i \in \{1 \dots \text{len}(X)\}$  do
19:     neighbors  $\leftarrow \mathcal{N}_i$ 
20:      $D_i \leftarrow$  distances between  $X[i]$  and  $X[\text{neighbors}]$ 
21:      $d_i \leftarrow$  distances between  $Y[i]$  and  $Y[\text{neighbors}]$ 
22:     stress  $\leftarrow$  stress +  $\|D_i - d_i\|$ 
23:      $\delta_i \leftarrow$  update force with MDS gradient from  $D_i$  and  $d_i$ 
24:   end for
25:    $Y \leftarrow Y + \delta$ 
26: end procedure

```

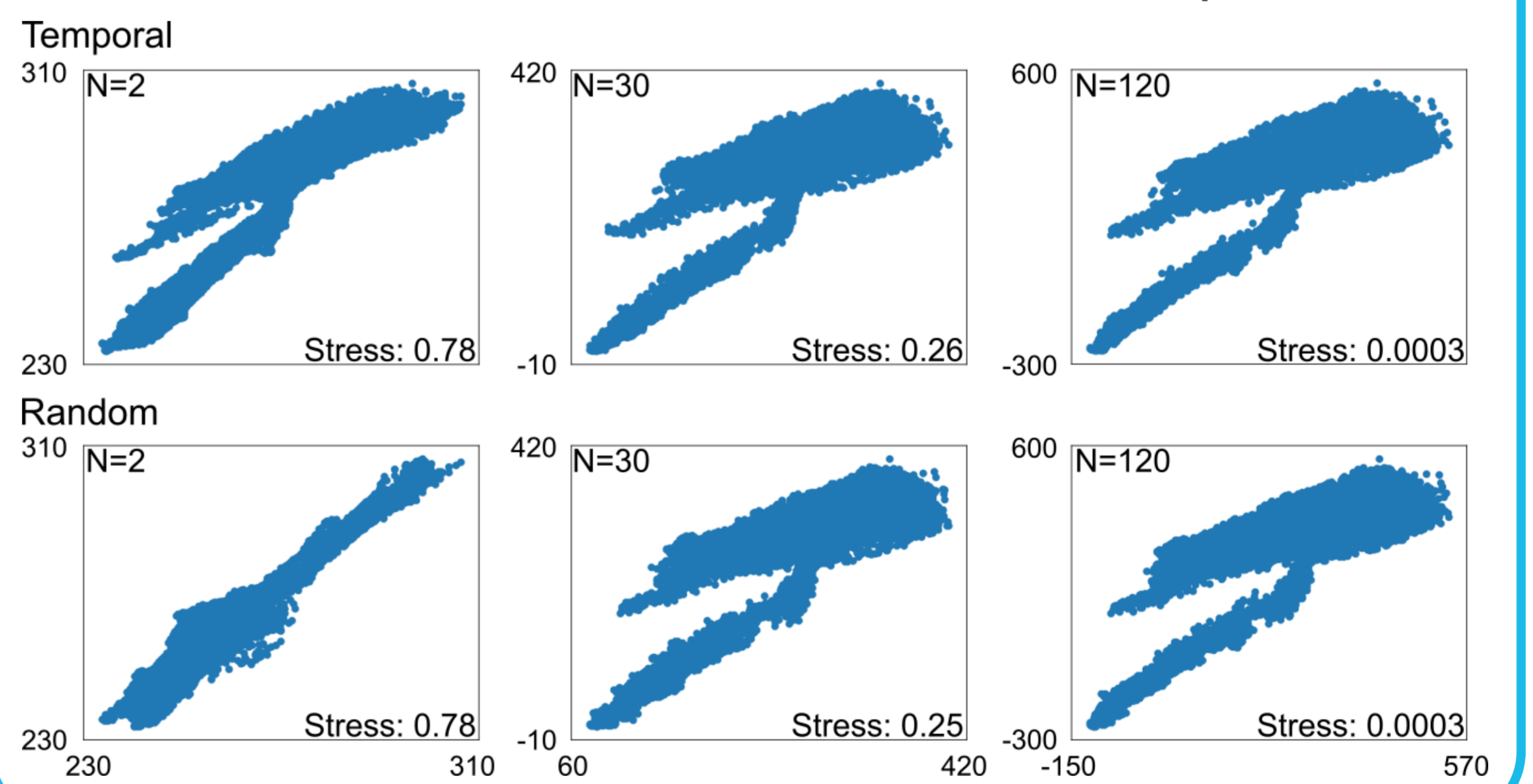
Runtime and Quality

- One step of progressive Glimmer is faster than the original Glimmer algorithm
- Stress converges to good results that can outperform the original algorithm



Influence of Sampling Order

- Application to MPI-GE climate ensemble in different sampling orders
- Progressive visualization in temporal order or choosing random time steps does not show differences in the decrease of stress
- Intermediate results differ for the first steps



Future Work

- Increase computation speed by using GPU
- Improve quality estimation
- Explore application scenarios including interactive steering of the visualization process

[1] S. Ingram, T. Munzner, and M. Olano. Glimmer: Multilevel MDS on the GPU. IEEE TVCG, 15(02):249–261, 2009.